Ncert Solution Chapter 4 Quadratic Equations Exercise 4.1

Question 1. Check whether the following are Quadratic Equations.

$$(i)(x+1)^2 = 2(x-3)$$

$$(ii) x^2 - 2x = (-2)(3-x)$$

$$(iii)(x-2)(x+1) = (x-1)(x+3)$$

$$(iv)(x-3)(2x+1) = x(x+5)$$

$$(v)(2x-1)(x-3) = (x+5)(x-1)$$

$$(vi)x^2 + 3x + 1 = (x-2)^2$$

$$(vii)(x+2)^3 = 2x(x^2-1)$$

$$(viii) x^3 - 4x^2 - x + 1 = (x-2)^3$$

Solution (i)

We just check degree of equation. If, degree of equation is equal to 2 then only it is a quadratic equation.

$$(x+1)^2 = 2(x-3)$$
 { $(a+b)^2 = a^2 + 2ab + b^2$ }
 $\Rightarrow x^2 + 1 + 2x = 2x - 6$
 $\Rightarrow x^2 + 7 = 0$

Degree of equation is 2. Therefore, it is a Quadratic Equation.

Solution (ii)

$$x^{2}-2x = (-2)(3-x)$$

$$\Rightarrow x^{2}-2x = -6+2x$$

$$\Rightarrow x^{2}-2x-2x+6 = 0$$

$$\Rightarrow x^{2}-4x+6 = 0$$

Degree of equation is 2. Therefore, it is a Quadratic Equation.

Solution (iii)

$$(x-2)(x+1) = (x-1)(x+3)$$

$$\Rightarrow x^2 + x - 2x - 2 = x^2 + 3x - x - 3 = 0$$

$$\Rightarrow x^2 + x - 2x - 2 - x^2 - 3x + x + 3 = 0$$

$$\Rightarrow x - 2x - 2 - 3x + x + 3 = 0$$

$$\Rightarrow -3x + 1 = 0$$

Degree of equation is 1. Therefore, it is not a Quadratic Equation.

Solution (iv)

$$(x-3)(2x+1) = x(x+5)$$

$$\Rightarrow 2x^2 + x - 6x - 3 = x^2 + 5x$$

$$\Rightarrow 2x^2 + x - 6x - 3 - x^2 - 5x = 0$$

$$\Rightarrow x^2 - 10x - 3 = 0$$

Degree of equation is 2. Therefore, it is a quadratic equation.

Solution (v)

$$(2x-1)(x-3) = (x+5)(x-1)$$

$$\Rightarrow 2x^2 - 6x - x + 3 = x^2 - x + 5x - 5$$

$$\Rightarrow 2x^2 - 7x + 3 - x^2 + x - 5x + 5 = 0$$

$$\Rightarrow x^2 - 11x + 8 = 0$$

Degree of Equation is 2. Therefore, it is a Quadratic Equation.

Solution (vi)

$$x^{2} + 3x + 1 = (x - 2)^{2} \qquad \{(a - b)^{2} = a^{2} - 2ab + b^{2}\}$$

$$\Rightarrow x^{2} + 3x + 1 = x^{2} + 4 - 4x$$

$$\Rightarrow x^{2} + 3x + 1 - x^{2} + 4x - 4 = 0$$

$$\Rightarrow 7x - 3 = 0$$

Degree of equation is 1. Therefore, it is not a Quadratic Equation.

Solution (vii)

$$(x+2)^{3} = 2x(x^{2}-1)$$
 {\((a+b)^{3} = a^{3} + b^{3} + 3ab(a+b)\)}
\(\Rightarrow x^{3} + 2^{3} + 3(x)(2)(x+2) = 2x(x^{2}-1)\)
\(\Rightarrow x^{3} + 8 + 6x(x+2) = 2x^{3} - 2x\)
\(\Rightarrow 2x^{3} - 2x - x^{3} - 8 - 6x^{2} - 12x = 0\)
\(\Rightarrow x^{3} - 6x^{2} - 14x - 8 = 0\)

Degree of Equation is 3. Therefore, it is not a quadratic Equation.

Solution (viii)

$$x^{3} - 4x^{2} - x + 1 = (x - 2)^{3} \qquad \{(a - b)^{3} = a^{3} - b^{3} - 3ab(a - b)\}$$

$$\Rightarrow x^{3} - 4x^{2} - x + 1 = x^{3} - 2^{3} - 3(x)(2)(x - 2)$$

$$\Rightarrow -4x^{2} - x + 1 = -8 - 6x^{2} + 12x$$

$$\Rightarrow 2x^{2} - 13x + 9 = 0$$

Degree of Equation is 2. Therefore, it is a Quadratic Equation.

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